ENEE 661 Spring 2013 Homework I. due date February 7 (Thursday)

1. For cure $Y: [t_0, t_f] \rightarrow \mathbb{R}^3$ t $\mapsto Y(t)$ show that curvature and torsion take the form

2 = x.(xxx) ||xxx||2

2. Show that the collection of matrices of the form

0 0 a23 0 0 0 1 0 0 0 0 a44

with any \$0 is a matrix (Lie) group.

Determine a basis for its Lie algebra,
and associated structure constants.

3. Show that the smallest Lie algebra of matrices which contains the matrices A, Az: $A_1 = \begin{pmatrix} 0 \\ 0 \end{pmatrix} ; \quad A_2 = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$ is four dimensional. Let the \$\overline{\Phi}\$ (t) be a smooth curve in Sl(h; IR), Show that we can $\dot{\Phi}(t) = \dot{\Phi}(t) \xi(t)$ where 3(t) has Zero trace +t. 5. Let t > \$ (t) be a smooth curve in se SE (n; IR) the special Euclideau growt of matrices of the form (A | b) where A & SO(h), b & R" and there is a now of zero's below A. Show that the associated Lie algebra is made up of motrices of the form (219) where $\Omega = R$ and $\gamma \in \mathbb{R}^n$ For n=3 determine all structure constants in a suitable natured basis for this

Lie algebra, devoted as se (3; IR)