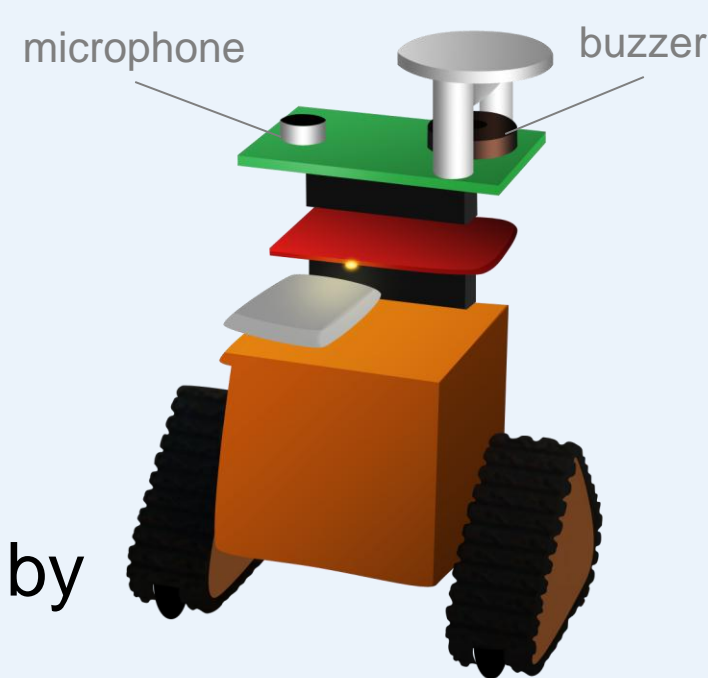




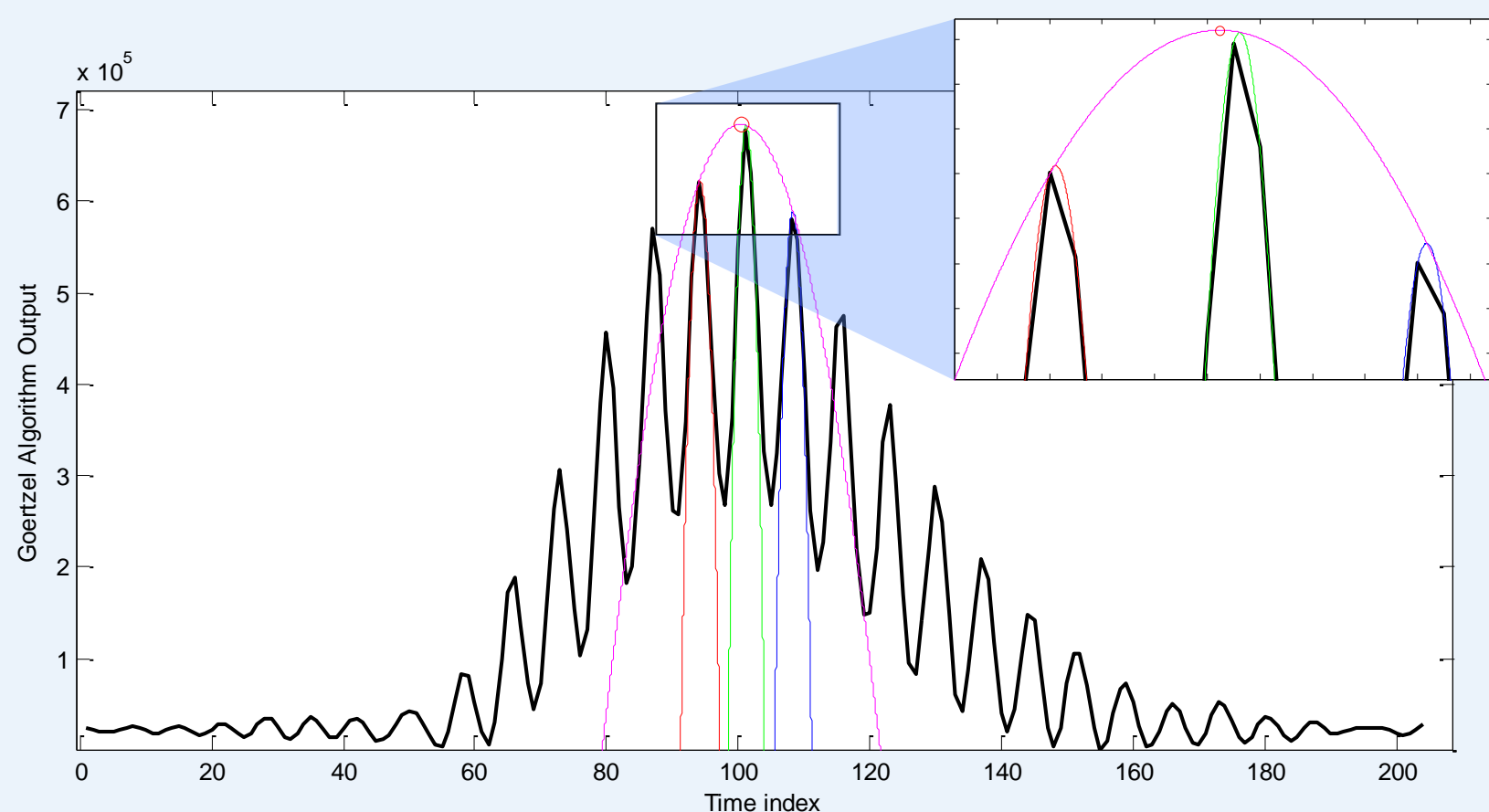
Goals

- Have a swarm of mini-robots follow a leader using distance-only sensors
- Refine distance sensor resolution through signal envelope interpolation
- Improve spatial awareness by incorporating odometry



Distance Sensing

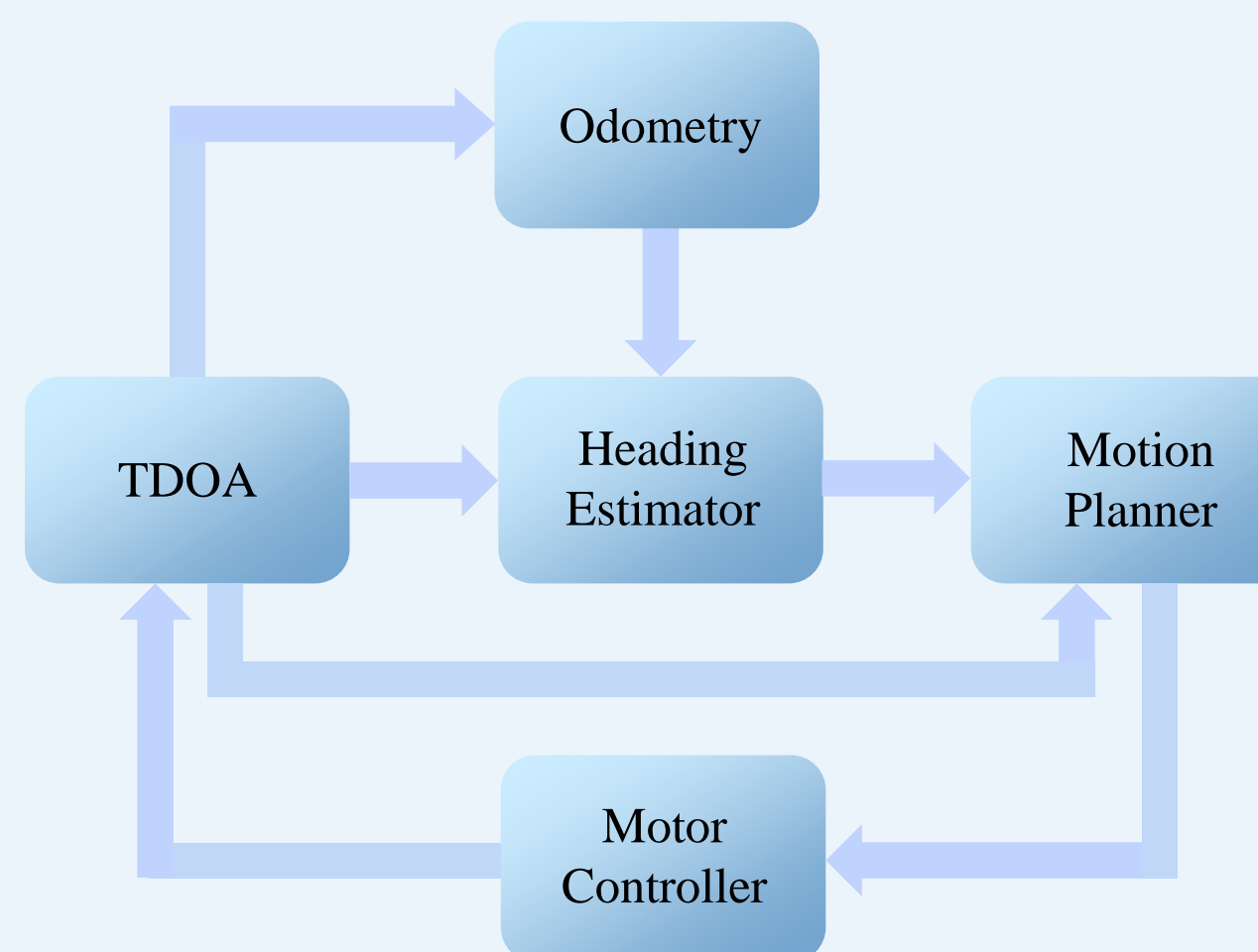
- **Time Difference of Arrival (TDOA)**
 - **Transmission:** leader robot emits a 12kHz sound pulse and a RF packet simultaneously
 - **Reception:** RF packet reaches the follower and instructs the microphone to start listening for pulse
 - **Filtering:** Goertzel algorithm detects the frequency of interest in the audio signal
 - **Interpolation (Goertzel waveform):** allows a better estimate for the time index at which the pulse occurred (peak of parabola)



Goertzel output interpolation using three peaks.

System Overview

- **Time Difference of Arrival (TDOA):** estimates how far away the leader is located
- **Odometry:** keeps track of the robot's position over time
- **Heading Estimator:** uses the Law of Cosines to estimate the angle between the follower and the leader
- **Motion Planner:** concerned with planning the path in terms of angle and distance
- **Motor Controller:** drives the motors according to the planned motion



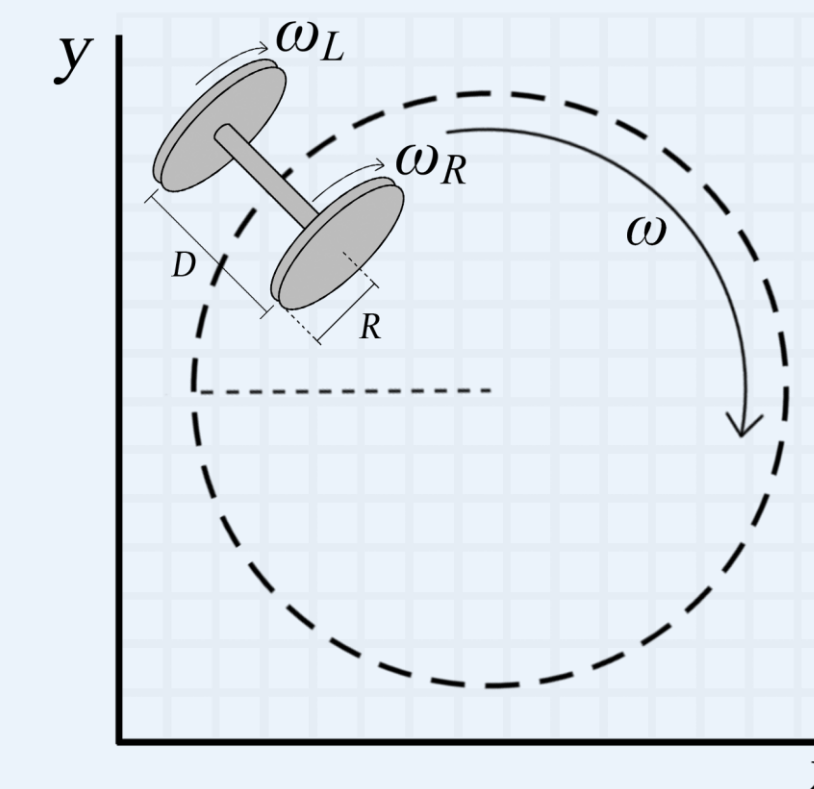
Conclusions

- Integrating interpolation in peak detection yields a better distance sensor resolution.
- | Method | Mean Resolution |
|------------------|-----------------|
| No Interpolation | 1.06 cm |
| Interpolation | 0.84 cm |
- Even though the robot is limited to a distance sensor only, it is possible to control its motion and position over time.

Motor Calibration

$$\omega = R \frac{(\omega_L - \omega_R)}{D}$$

$$v = R \frac{(\omega_L + \omega_R)}{2}$$



- **Calibration:** finding the linear relationship between the applied voltage and the resulting angular and forward velocities (twist)

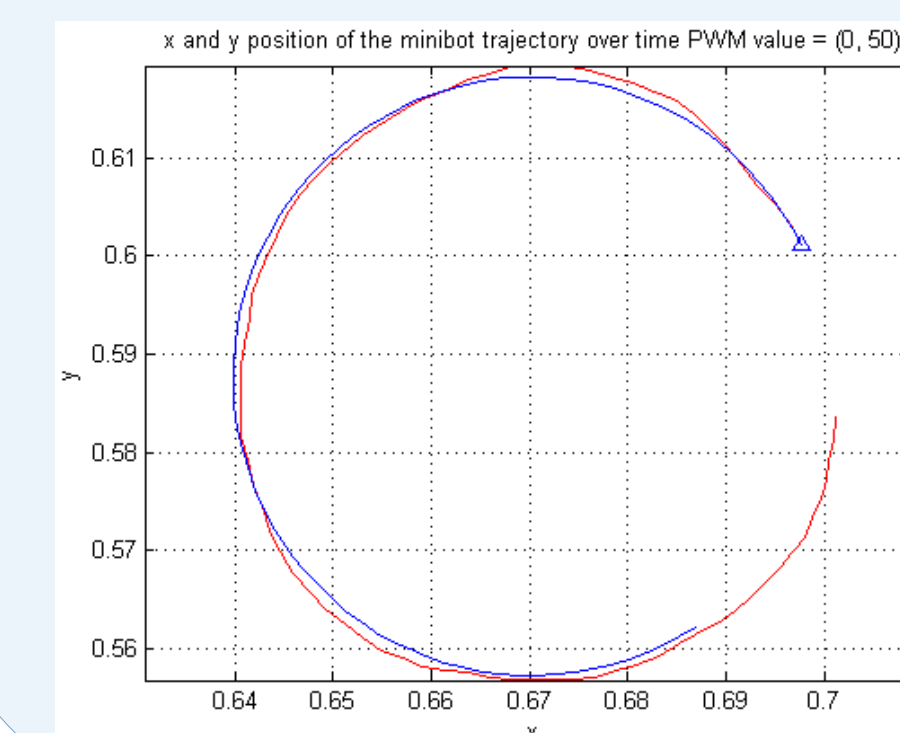
$$\begin{bmatrix} v \\ \omega \end{bmatrix} = A \begin{bmatrix} \omega_L \\ \omega_R \end{bmatrix}$$

- Matrix A is found by tracking the robot's trajectory for a given voltage input

Odometry

- **Odometry:** describes the final position of the robot for a specific command
- Allows control and prediction of the robot's motion for heading estimation
- The equations of motion are:

$$\begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} v \cos(\theta) \\ v \sin(\theta) \\ \omega \end{bmatrix}$$



Simulation (blue line)
Actual Trajectory (red line)

